Homework 4

CS 181, Fall 2022

Out: Nov. 16 **Due**: Nov. 22, 11:59 PM

Problem 0: Readings

The following sections of the Barton textbook chapter, which can be found on the resources page of the course website under Chapter 3 Readings. They may be helpful for Problems 3 and 4.

- (a) For Distance Methods, Corrections Are Essential to Convert Measures of Similarity to Evolutionary Distances, pgs. 27 29
- (b) UPGMA and Neighbor-Joining Methods, pgs. 22 26

Problem 1: Building and using suffix trees

The CS 181 TAs take a special trip to the aquarium because entry is free for college students today! When they arrive, it turns out they have to solve a special problem in order to gain entry. They must find all the suffizes of the word, "aquaquarium", and they're enlisting your help to do so!

- (a) Construct the **expanded** suffix tree T_x for the word x = AQUAQUARIUM. Build the tree one suffix at a time, starting with suf₁. Show the first four partial trees in your construction as well as the complete suffix tree T_x .
- (b) Show how to use your suffix tree to return the starting indices of all occurrences of the string QUA in the text x. List all of these indices. In general, what is the big-O time complexity of returning the starting indices of all occurrences of a pattern p in a text t? Explain.
- (c) Show how to use your suffix tree to determine whether the string QUALITY occurs in x. Does it occur in x? In general, what is the big-O time complexity of determining whether a pattern p occurs in a text t? Explain.
- (d) Bonus: Construct the compacted suffix tree and the position suffix tree for the word x = AQUAQUARIUM. Explain why position suffix trees can be stored in O(n) space, whereas compact suffix trees require $O(n^2)$ space.

Problem 2: Longest shared substring

Consider the following problem:

LONGEST SHARED SUBSTRING PROBLEM
Input: Strings u and v.
Output: The longest substring that occurs in both u and v.

In class, it was briefly mentioned that we could solve this problem by concatenating the two strings and constructing a joint suffix tree for the resulting string. In this problem, we expand upon this idea.

We begin by appending two different end-of-string characters to u and v, giving us u# and v^{\$}. We then build the suffix tree for the concatenation of these two strings, u#v^{\$}. We shall color the leaves of this tree according to the following rule: if a leaf is labeled by the starting position of a suffix starting in u, color it blue; if a leaf is labeled by the starting position of a suffix starting in v, color it red. Note that all the leaves in the tree will be colored either red or blue according to this procedure.

Next we color the internal nodes of the tree according to the following rules:

- A node is colored blue (resp. red) if all the leaves in the subtree rooted at that node are blue (resp. red).
- A node is colored purple if the subtree rooted at that node contains both blue and red leaves.

For <u>all</u> tasks in this problem, assume that we are using **expanded** suffix trees.

- (a) Explain how every path ending in a purple node in the suffix tree of u # v spells out a substring shared by u and v.
- (b) Explain how every path ending in a blue (resp. red) node in the suffix tree of u # v\$ spells out a substring that appears in u but not in v (resp. v but not in u).

Given these two facts, it should be clear how we find the longest shared substring of u and v: We need only examine the strings spelled by paths that lead to purple nodes; the longest such string is precisely the solution to the Longest Shared Substring Problem.

The above approach makes use of a single suffix tree to solve the Longest Shared Substring Problem. It is also possible to solve this problem using two suffix trees, one for each of u and v.

- (c) Describe an algorithm that solves the Longest Shared Substring Problem using the two suffix trees T_u and T_v .
- (d) Compare (in as much detail as possible) the worst case space- and time-efficiency of the algorithm that uses a single suffix tree for u # v with the worst case space- and time-efficiency of the algorithm you designed in (c) above.

Problem 3: Jukes-Cantor Distance

(a) To get the feel of how to calculate the Jukes-Cantor distance, consider two biological sequences that have accumulated mutations over time. Below are snapshots of the two sequences at 4 different points in evolutionary time:

	t = 1	t=2	t = 3	t = 4
Sequence 1	AGGTCA	AGCTCA	AGCTCA	AACTCA
Sequence 2	AGGTCA	AGGTCA	TGGTCA	TGGTCC

For each timepoint t, calculate the fraction of sites that are different between the two sequences, λ_t . Then use this value to calculate the Jukes-Cantor distance D_t between each sequence.

(b) Now consider a fifth timepoint:

	t = 5
Sequence 1	AACTGA
Sequence 2	TGGTCC

Compute λ as above. What happens when you try to use this value to calculate the Jukes-Cantor distance?

(c) Propose a correction to the Jukes-Cantor distance that avoids the issue above. What result do you get when you calculate your new distance at t = 5? Explain in two or three sentences the potential benefits and drawbacks of your new distance. It may be helpful to read up a little on the *Infinite Sites Model*.

Problem 4: Neighbor Joining

During a special trip to the New England Aquarium, the CS181 TAs take a short boat ride to the Stellwagen Bank National Marine Sanctuary. One of the world's most active marine sanctuaries, Stellwagen Bank is abundant with whales, dolphins, sea birds, and other marine life. They are lucky enough to see many marine creatures. Wanting to better understand the evolution of marine mammals over the decades, one of the TAs decides to build an evolutionary tree for various mammals.

	Whale	Dolphin	Porpoise	Narwal	Beluga
Whale					
Dolphin	135				
Porpoise	159	24			
Narwal	213	78	54		
Beluga	177	42	18	36	

Use the distance matrix above and the neighbor joining algorithm to construct an evolutionary tree for the marine mammals above. In a sentence or two, comment on Beluga's place in the evolution of marine mammals.

Problem 5: Ethics of HIV Phylogenetics

Molecular HIV Surveillance (MHS) refers to the use of phylogenetic methods to detect and understand patterns of HIV transmission, and particularly to detect clusters of individuals with genetically-linked strains of HIV.

One application of MHS data is to HIV cluster detection and response (CDR), which is defined by the CDC as "the actions taken to prevent further transmission when a growing cluster of HIV transmission and its associated risk network is detected." CDR has been identified as a crucial pillar of a federal initiative to End the HIV Epidemic by 2030.

Review Molldrem and Smith (2020), an article which criticizes the use of Molecular HIV Surveillance (MHS) data in HIV cluster detection and response (CDR).

- a. Read the section titled "History and Context for MHS and CDR". Then answer the following questions.
 - i. What characteristic of HIV makes phylogenetics a possible tool for studying the virus? (1-2 sentences)
 - ii. Briefly explain how HIV surveillance data is used in CDR programs in your own words. (1-2 sentences)
- b. Read the section "Theoretical Framing: From 'Critical Bioethics' to 'Bioethics of the Oppressed'". Then answer the following questions.
 - i. Explain your understanding of "Data Justice" as a critical framework (2-3 sentences). (Optional: If you would like further reading, you can take a look at page 874 of this article)
 - ii. How does "Data Justice" as a framework for analyzing ethical issues differ from ethical theories we have discussed previously in the class (3-4 sentences)?
 - iii. The article explains that blood samples from HIV-positive patients are routinely collected in order to identify whether a patient's particular strain of HIV is resistant to certain antiviral drugs. However, the "[r]e-uses of clinical HIV data for public health surveillance and prevention do not require consent." Do you believe this practice is ethical? Please use at least one of the three ethical frameworks (utilitarianism, Kantian deontology, Data Justice) in justifying your response (4-5 sentences).
- c. Read the section "Case 2: Determining Directionality of Transmission".
 - i. Explain how the way phylogenetic relationships are represented in tools such as HIV-TRACE may imply the directionality of HIV transmission (1-2 sentences).
 - ii. Brainstorm one or two ways you could redesign tools like HIV-TRACE to make them less vulnerable to misinterpretation such as directionality of transmission (3-4 sentences). (Your answer may consider any aspect of the tool, including the visual representation of the phylogenetic relationships. We're not looking for a specific, or fully-fleshed out solution here, just brief thoughts which reflect thoughtful engagement with the question).